

A prediction of the longevity of the Lusi mud eruption, Indonesia

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Abstract

A mud eruption, nicknamed Lusi, began near Sidoarjo, East Java, in May 2006. It has discharged $\sim 10^4 - 10^5$ m³/day of mud ever since. In order to understand the nature of the eruption and its potential longevity, we develop a model for the coupled evolution of the mud source and ascent of mud through a conduit to the surface. The ascent of the mud is driven by overpressure in the mud source and by the exsolution and expansion of dissolved gases. We assume that erupted fluids originate in the mud source region. Mobilization of the mud is caused by elastic stresses induced by mud evacuation from the subsurface. We perform Monte Carlo simulations to explore model outcomes while perturbing the unknown material properties of the mud and surrounding medium. Using our preferred model, we calculate a 50% chance of the eruption lasting <41 years and a 33% chance that it lasts >84 years. Eruptions often end with the formation of a caldera, but longer eruptions are less likely to form a caldera. Model predictions can be refined with additional, but currently unavailable constraints: more precise estimates of

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mud discharge, the yielding behavior of the materials in the subsurface, total gas content in the mud source, and identification of any erupted fluids that do not originate in the mud source.

1. Introduction

On 29th May, 2006 an eruption of mud and fluids occurred in Sidoarjo, Indonesia, creating a mud eruption named Lusi (short for Lumpur Sidoarjo). Approximately $10^4 - 10^5$ m³/day of mud has erupted ever since (Mazzini et al., 2007), displacing >60,000 people (Bayuni, 2009). The large and active subsidence created by the eruption continues to damage transportation and communication infrastructure.

The birth and evolution of the Lusi eruption are well documented (Istadi et al., 2009; Mazzini et al., 2007) providing a special opportunity to study how and why large mud eruptions occur (Davies et al., 2007). Because the eruption occurred next to a 3 km deep gas exploration well, we also have unique insight into the subsurface lithology and properties immediately prior to the eruption. Specifically, we can constrain the source of the mud, origin of erupted fluids, and the driving mechanism of the eruption.

In this study, we develop a mechanical model for the Lusi eruption that couples mud transport to the surface through a conduit with the evolution of the mud source at depth. The model is analogous to those used for magmatic volcanoes in that there is a mud chamber and a conduit, and dissolved gases play a key role in sustaining the eruption. It differs in that the volume of mobilized mud (analogous to eruptible magma at a volcano) increases over time, owing to progressive mobilization of mud in the source region. We begin by summarizing some of

22 the key observations that guide model development. Next, we describe the model
23 and governing equations. We end by predicting the longevity of the eruption and
24 outline how to test and improve the model.

25 **2. Observational Constraints**

26 Microfossils imply a mud source in the upper Kalibeng formation, occurring
27 at depths between 1220-1860 m, which consists of Pleistocene clay (Sawolo et
28 al., 2009). The observed clay mineralogy is most similar to mud from 1600-1800
29 m (Mazzini et al., 2007). Kerogen compositions of erupted mud are also similar
30 to those obtained from side-wall cores taken at a depth of 1707 m (Sawolo et al.,
31 2009). Drilling logs indicate that the Kalibeng formation is under-compacted and
32 over-pressured, with porosity of about 30% (Istadi et al., 2009; Tanikawa et al.,
33 2010). There is some controversy over the porosity of the Kalibeng formation.
34 Based on density logs from the well Banjar Panji-1 (BJP1) Davies et al. (2011a)
35 estimate lower porosities (10-13%), which would necessitate an external water
36 source.

37 While there is no debate about the source of mud, there is considerable dis-
38 agreement about the source of fluid. The water content of the mud during the
39 earliest stages of eruption was 60-70% (Mazzini et al., 2007; Istadi et al., 2009).
40 This is greater than the porosity of the Kalibeng formation, $\sim 30\%$, implying an
41 additional source of fluid. Davies et al. (2007) suggest that water is sourced from
42 a carbonate aquifer at depths of 3 km. Mazzini et al. (2007) suggest that the pri-
43 mary source of water is diagenesis and dehydration within the source region of
44 the erupted mud. The lower concentrations of B, Li, and Cl, as well as the $\delta^{18}\text{O}$
45 enrichment of the water, can be explained by clay dehydration. Carbon isotope

46 measurements of hydrocarbons and methane in the erupted mud indicate the pres-
47 ence of both biogenic methane, which could be produced in the source muds, and
48 thermogenic methane, which, along with heavier hydrocarbons and H_2S , must
49 have migrated from greater depths (Mazzini et al., 2007). The migration could
50 have preceded the eruption.

51 The reported water content of the erupting mud provides an additional con-
52 straint. While the initial water content was high, 60-70% (Bayuaji et al., 2009),
53 it gradually decreased to 30% over the first year (Mazzini et al., 2007). As this
54 value is similar to the porosity of the source layer, we assume there is no signifi-
55 cant addition of fluids to the mud source during the bulk of the eruption.

56 The temperature of the erupting mud is 70-100 °C (Sawolo et al., 2009). The
57 geotherm measured in the BJP1 (~200 m from the site of the eruption) is 42°C/km
58 and the mean annual air temperature is 27°C (Bayuaji et al., 2009); temperatures
59 of 100 °C are reached at depths of 1700 m (Mazzini et al., 2007). The observed
60 mud temperature does not require the addition of significant amounts of fluid hot-
61 ter than the temperature at the source depth of the mud.

62 **3. Model**

63 We develop a model that is motivated and constrained by these observations.
64 The fluids, mud and gas for the bulk of the eruption are sourced from the Kalibeng
65 formation. Additional fluids may have played a key role in the initiation (Davies
66 et al., 2007; Tingay et al., 2008) and during the early stages of the eruption, but
67 will not influence subsequent dynamics, evolution, and longevity.

68 Our model is conceptually similar to typical models for magmatic volcanoes
69 in that the system consists of a “chamber” coupled to a “conduit”. It differs, how-

70 ever, in the nature and origin of the chamber component as well as the boundary
 71 condition imposed on the conduit at the surface. For magmatic volcanoes and
 72 some mud volcano models (Zoporowski and Miller, 2009), the chamber boundary
 73 is a material surface and the chamber volume changes owing to influx or outflux
 74 during the eruption. In our model, an initially spherical chamber consists of mobi-
 75 lized mud – mud with a rheology that allows it to flow and to erupt. This chamber
 76 is surrounded laterally by mud of the same composition that has not yet become
 77 mobilized. The lateral extent of the mud chamber is therefore defined by a rheo-
 78 logical, rather than a compositional, transition and evolves over time (Figure 1).
 79 Mud erupts through a cylindrical conduit, driven by gas exsolution and expansion
 80 and by chamber overpressure.

81 *3.1. Mud Source*

82 We model the mud chamber as a cylindrical cavity of thickness 600 m cen-
 83 tered at a depth of 1500 m. The edges of the cavity are rounded (Figure 1), and
 84 the radius of curvature remains constant as the chamber expands. The details of
 85 the assumed chamber geometry (e.g. radius of curvature of the edges) are less
 86 important than the aspect ratio, which exerts the dominant control on the stress
 87 concentration near the lateral boundary of the chamber. For the purposes of cal-
 88 culating stresses outside the chamber, we assume that the continuum surrounding
 89 the chamber is a linear elastic solid over the time scale of the eruption. Stresses
 90 are governed by

$$\nabla \cdot \underline{\sigma} = \underline{0}, \quad (1)$$

91 where $\underline{\sigma}$ is the Cauchy stress, related to strain ($\underline{\epsilon}$) through the constitutive equation

$$\sigma_{ij} = \lambda \epsilon_{kk} \delta_{ij} + 2\mu \epsilon_{ij}. \quad (2)$$

92 Here λ and μ are the Lamé constants. The model domain is subject to stress
 93 boundary conditions at the chamber wall (∂S) and free surface ($z = 0$):

$$\sigma_n|_{\partial S} = \Delta P_C \quad (3)$$

94

$$\sigma_n|_{z=0} = \sigma_t|_{z=0} = 0. \quad (4)$$

95 Here σ_n and σ_t are the normal and tangential stresses, respectively. ΔP_C is equal
 96 to the difference between the current pressure in the mud source layer $P_C(t)$ and
 97 the initial source pressure, $P_C(0)$, and obeys the equation of state of the material in
 98 the chamber, described later. We calculate elastic stresses and strains numerically,
 99 using the axisymmetric program mode in FEAP, version 8.3 (Taylor, 2008). We
 100 assume an isotropic initial stress state, neglecting any effects arising from devia-
 101 toric tectonic stresses.

102 The equation of state relates specific volume v_S (volume per unit mass) of the
 103 3-phase mixture inside the chamber to pressure P . If we denote the undeformed
 104 volume of the cavity $V_{0,C}$ and the deformed volume of the cavity V_C , the pressure
 105 satisfies

$$\rho_0 V_{0,C} + \int_0^t \dot{M}(\tau) d\tau = V_C(P)/v_S(P) \quad (5)$$

106 where \dot{M} is the time derivative of chamber mass, which is the opposite of the
 107 eruptive mass discharge, and ρ_0 is the in-situ density of the mud at the initial
 108 chamber pressure. We perform Newton-Raphson iteration to obtain a chamber
 109 pressure that is consistent with the deformed volume of the cavity, the equation of
 110 state of the material inside the chamber, and the mass of material remaining in the
 111 chamber.

112 We adopt a von Mises yield stress (and equivalently, strain) criterion for mo-
 113 bilizing additional mud from the chamber's surroundings. The von Mises stress

114 is

$$\sigma_v = \sqrt{3J_2}, \quad (6)$$

115 where J_2 is the second deviatoric stress invariant. As mud erupts from the cham-
 116 ber, the chamber deflates and its pressure decreases, producing stresses in the
 117 surrounding mud. Once the von Mises stress in the unmobilized part of the mud
 118 layer exceeds a critical value $\sigma_{y, \text{chamber}}$ we assume that additional mud is mobi-
 119 lized and becomes part of the chamber. We solve for the expanding chamber
 120 radius iteratively so that the von Mises stress at the perimeter of the chamber is
 121 everywhere less than the yield stress. The von Mises stress criterion has been used
 122 to model mud yielding in other studies (e.g. Mazzini et al., 2009) and is the best
 123 higher-dimension analogue to the yielding criterion used to study mudflows in one
 124 dimension (e.g. Marr et al., 2002).

125 3.2. Conduit

126 Mud rises through a conduit towards the surface. The driving force is provided
 127 by a combination of mud chamber overpressure, and exsolution of dissolved gas
 128 and expansion of vapor during decompression and ascent. We model conduit pro-
 129 cesses assuming steady one-dimensional multiphase flow through a cylinder (e.g.
 130 Mastin, 2002; Dobran, 2001), subject to conservation of mass and momentum:

$$\frac{\partial}{\partial z} (\rho_{\text{mix}} u) = 0 \quad (7)$$

131

$$\frac{\partial P}{\partial z} = \frac{-\rho_{\text{mix}} \left(g + \frac{8\mu u}{\rho_{\text{mix}} r^2} \right)}{1 - \frac{u^2}{c^2}}. \quad (8)$$

132 In equations 7-8, u is the mixture velocity of mud plus gas, P is the pressure,
 133 g is gravity, μ is mud viscosity, r is the conduit radius. We note that the term
 134 $(8\mu u)/(\rho_{\text{mix}} r^2)$ can be interpreted as a friction factor, and any change to conduit

135 geometry (e.g. opening of multiple vents or widening/collapse of the main vent)
 136 would simply change the functional form of this term. ρ_{mix} is the mixture density,
 137 given by:

$$\rho_{mix} = \left(\frac{n}{\rho_g} + \frac{1-n}{\rho_l} \right)^{-1} \quad (9)$$

138 with n the mass fraction of gas, ρ_g and ρ_l the densities of gas and water plus
 139 particles respectively.

$$c = \left(\frac{\partial P}{\partial \rho_{mix}} \right)_S^{1/2} \quad (10)$$

140 is the sound speed of the mixture, calculated numerically to ensure mass conser-
 141 vation.

142

143 Equations 7-8 are solved with a bisection and shooting method and 4th order
 144 Runge-Kutta integration to satisfy two boundary conditions: a one-way coupling
 145 to the chamber pressure evolution at the base of the conduit

$$P(z = -H) = P_C \quad (11)$$

146 and an atmospheric pressure boundary condition at the surface

$$P(z = 0) = P_{atm} \quad (12)$$

147 We assume that gas bubbles are dynamically coupled to the flow until a critical
 148 porosity (gas volume fraction) of 0.3 is reached (Blower, 2001; Saar and Manga,
 149 1999), which we take as the threshold permeability for gas loss. This limits the
 150 acceleration of mud in the conduit and effectively ensures that velocities never
 151 approach the sound speed of the mixture. We also assume that the water and mud
 152 particles are dynamically coupled. Tanikawa et al. (2010) estimate permeabili-
 153 ties of 10^{-20} to 10^{-19} m² in the Upper Kalibeng Formation. Assuming a driving

154 pressure gradient of 10 MPa/km (estimated from chamber overpressure and con-
155 duit length scale), we compute the pore fluid velocity as $v = -k/(\mu\phi)\nabla P = 10^{-12}$
156 m/s, many orders of magnitude smaller than the bulk velocity of the multiphase
157 mixture.

158 The reservoir (chamber) enthalpy for a given initial temperature (T) and pres-
159 sure (P) is calculated using the XSteam (www.x-eng.com) implementation of the
160 International Association for the Properties of Water and Steam (IAPWS) IF-97
161 steam tables. We assume that the ascending mixture experiences isenthalpic de-
162 compression during transport (e.g. Lu and Kieffer, 2009), allowing us to calculate
163 $T(z)$ from conservation of enthalpy and the steam tables. Once the P-T decom-
164 pression path is known, we calculate the density and mass fraction of liquid and
165 gas phases, which are functions of T and P , using the $\text{CH}_4\text{-H}_2\text{O}$ equation of state
166 developed by Duan et al. (1992a,b) and implemented in HCO-TERNARY (Nieva
167 and Barragan, 2003) and the online calculator at geotherm.ucsd.edu. It is through
168 this calculation that we account for changes in density due to gas exsolution and
169 expansion, and we emphasize that the gas solubility is accounted for through the
170 $\text{CH}_4\text{-H}_2\text{O}$ equation of state and that the conversion of liquid water to vapor during
171 ascent is limited by conservation of enthalpy.

172 4. Model Parameters

173 Our model contains a number of geometric and material properties, some that
174 are well-constrained and others that are poorly constrained and treated as vari-
175 ables. The following have enough uncertainty to be treated as variables: failure
176 strength of mud adjacent to the chamber ($\sigma_{y,\text{chamber}}$), failure strength of the near-
177 surface material ($\sigma_{y,\text{caldera}}$), Young's modulus (E), and Poisson's ratio (ν).

178 4.1. Constants

179 Mud viscosity μ and conduit radius r affect mud ascent through the grouping
180 μ/r^2 . Manga et al. (2009) measured mud viscosity of 10^5 Pa·s on sample JV07-05
181 (Mazzini et al., 2007) of Lusi mud with 43 wt.% water. Water content has a large
182 effect on viscosity. Rifai (2008) measured viscosity of samples collected from
183 Lusi and found an approximately 80% increase in viscosity when water content
184 decreased from 62.5 wt.% to 59.0 wt.%. Rudolph and Manga (2010) measured
185 a fivefold increase in mud viscosity when water content decreased from 40 wt.%
186 to 33 wt.%. The geometry of the conduit through which the mud rises cannot
187 be observed directly. The initial fissure, observed within the first few days, was
188 hundreds of meters long and tens of centimeters wide at the surface (Mazzini et
189 al., 2007). Its burial by erupted mud does not allow us to determine how the con-
190 duct subsequently evolved and whether discharge became localized, as it does for
191 magmatic fissure eruptions. In March 2007, 10 months after the eruption began,
192 40 cm diameter concrete balls were able to reach depths of 1000 m (Mazzini et
193 al., 2007). As these balls had no effect on the eruption rate, their size provides a
194 minimum estimate of conduit dimensions. For a given dissolved gas concentra-
195 tion, we choose a combined conduit dimension and viscosity that reproduces the
196 observed 6×10^4 m³/day mean discharge (Tingay, pers. comm. 2010), empha-
197 sizing again that viscosity and conduit radius enter the problem only through the
198 grouping μ/r^2 .

199 The volume ratio of erupted gases is spatially and temporally variable. Mazz-
200 ini et al. (2007) measured gas composition at seeps near the crater and sampled
201 steam clouds emanating from the crater. The seeps discharge 80-85% CH₄ and
202 10-19% CO₂. The gas samples from the steam cloud are more variable, with CO₂

203 comprising 28-74% and CH₄ comprising 24-72% of the gas among three samples.
 204 In general, the CO₂-enriched samples are also enriched in C_X for X > 1. We in-
 205 terpret these measurements as indicating a methane-dominated gas composition,
 206 following two lines of reasoning. First, CO₂ (specific gravity 1.53) and CX, X> 2
 207 are denser than air while CH₄ is lighter than air (specific gravity 0.56). The steam
 208 samples were collected downwind of the crater, and some separation of gases by
 209 density may have occurred during transport. Second, we expect that the local
 210 gas seep chemistry, which is methane-rich, will be dominated by the composition
 211 of the erupting fluids. However, subsequent measurements may indicate that the
 212 erupting gas composition is CO₂-dominated (Mazzini, pers. comm. 2011). In
 213 our model, the gas composition is unimportant. As long as the discharge at ini-
 214 tial chamber pressure fits the observational constraint, the relationship between
 215 chamber pressure and discharge is independent of gas composition. We show
 216 this graphically in Figure 2. The only discrepancy in cumulative mass removed
 217 (Figure 2) for the model using CO₂ and the model using CH₄ arises from a small
 218 mismatch in flux, less than 5%, the tolerance that we chose when calculating con-
 219 duit velocities as a function of chamber pressure.

220 4.2. *Unknowns*

221 The value of $\sigma_{y,chamber}$ for the mud source is not known. Kopf et al. (2009)
 222 measured sediment shear strength in situ in the field (at the Dashgil mud volcano,
 223 Azerbaijan) using a Cone Penetration Test. They found strengths as low as 150
 224 kPa in the conduit and 300-700 kPa at other locations. We thus consider values
 225 of $\sigma_{y,chamber}$ with a mean of 1 MPa for the pre-mobilized mud, and a standard
 226 deviation of an order of magnitude in log-space. Once the mud loses strength and
 227 enters the chamber or flows in the conduit, we treat it as a viscous fluid. The value

228 of $\sigma_{y,caldera}$ is also unknown, and we assume that it is 10 times larger than $\sigma_{y,chamber}$.
 229 We experimented with values of $\sigma_{y,caldera}/\sigma_{y,chamber}$ as large as 100 but found it
 230 to be unimportant. We explore a range of values for E (Young's modulus) and ν
 231 (Poisson's ratio) for the surroundings centered about 10^8 Pa and 0.15, respectively,
 232 chosen to be consistent with the geodetic modeling of Fukushima et al. (2009).

233 The mean values and range of parameters used in the Monte Carlo simula-
 234 tions are summarized in Table 1. We considered three scenarios. In the first, our
 235 preferred model, we give more weight to values of unknown parameters near our
 236 preferred mean value by using gaussian distribution of random numbers. E and
 237 $\sigma_{y,chamber}$ have values that are normally distributed in log-space, i.e. $\log_{10}(\sigma_{y,chamber} \text{ (Pa)}) =$
 238 6 ± 1 . We also performed the same suite of Monte Carlo simulations with proba-
 239 bility density functions (pdfs) that are constant in the range $[mean - \sigma, mean + \sigma]$
 240 or $[mean - 2\sigma, mean + 2\sigma]$ and zero elsewhere. We refer to these as σ -boxcar and
 241 2σ -boxcar, respectively (Table 2).

242 5. Criteria to Terminate Eruption

243 The factors that cause eruptions to end are, in general, poorly understood. We
 244 consider two possible scenarios. First, the chamber pressure decreases (sometimes
 245 below lithostatic pressure) until there is insufficient potential energy available to
 246 drive the eruption. Alternatively, the eruption may end if the near-surface mate-
 247 rial fails, initiating caldera formation. The latter condition does not require that
 248 the eruption has ended, just that it has entered a regime in which our model is
 249 no longer applicable. Caldera formation occurs if continued removal of material
 250 induces failure of the overlying layers, and becomes more likely as the chamber
 251 grows and deviatoric stresses are concentrated between the surface and regions of

high curvature at the chamber walls. We evaluate J_2 (second deviatoric stress invariant) along a trajectory that begins at the tip of the mud chamber and progresses upward always in the direction of greatest J_2 . We then evaluate J_2 along this trajectory at half the chamber depth. If the value at this point is greater than $\tau_{y,caldera}$, we assume that a caldera forms. This method produces a conservative criterion for caldera formation because J_2 is greatest at the free surface and decreases with increasing depth.

6. Results

To predict longevity, we performed Monte Carlo simulations in which we perturbed the four unknown model parameters. We illustrate the evolution of chamber pressure, chamber radius, total mass removed, and mass flux as a function of time during an individual Monte Carlo realization in Figure 2. Of 2584 simulations, 1223 eruptions ended due to chamber underpressure, 725 formed a caldera, 397 lasted longer than 100 years (the maximum time allowed for computational purposes), and 239 produced unbounded chamber growth (which is not geologically reasonable, as the mud source has finite lateral extent). In general terms, eruptions that ended due to insufficient chamber pressure never incorporated additional mud into the chamber because $\sigma_{y,chamber}$ was large; those that produced unbounded growth had the lowest $\sigma_{y,chamber}$. Caldera formation was favored by larger E and low $\sigma_{y,chamber}$. Our mean $E = 10^8$ Pa (Fukushima et al., 2009) and $\sigma_{y,chamber}$ lie close to the line that divides model outcomes in E - $\sigma_{y,chamber}$ space (Figure 3). Poisson's ratio is unimportant.

Although short eruptions are the most frequent model outcome, the observation that Lusi has been erupting for more than 4.5 years provides an additional

constraint. If we exclude all eruptions shorter than 4.5 years and give equal weight to all durations greater than 4.5 years, we obtain a cumulative probability distribution (Figure 4). The gaussian model predicts that the eruption has a 33% chance of lasting <21 years, a 50% chance of lasting less than 40 years, and a 67% chance of lasting <84 years. The σ -boxcar and 2σ -boxcar model results are summarized in Table 2.

7. Discussion

Eruptions driven by overpressure have approximately exponentially decaying discharge because the mass removal decreases overpressure (Woods and Huppert, 2003). In contrast, to date the Lusi eruption has displayed a remarkably uniform discharge, varying only by less than a factor of ten over the first few years. Eruption rates are difficult to determine accurately and the Lusi eruption is no exception. In the first few months discharge was about 50,000 m³/day and increased to as much as 180,000 m³/day over the next year (Mazzini et al., 2009). Satellite observations are most consistent with average eruption rates of 90,000 m³/day (Istadi et al., 2009). Our model produces approximately constant eruption rates for a given conduit size because once the chamber begins expanding, the chamber pressure is buffered by incorporating additional material. Changes in observed eruption rates could reflect evolution of the conduit geometry or opening of new conduits, phenomena not captured by our model.

Mud volcanoes are known to form calderas (Kopf, 2008). Evans et al. (2008) describe mud calderas, both on land and submarine, with diameters of 1-2 km. Figure 3 shows that E and $\sigma_{y, \text{chamber}}$ are the key variables controlling caldera formation. Figure 5 is a histogram of eruption duration, also showing the breakdown

300 between eruptions that end due to chamber underpressure and eruptions culmi-
301 nating in the formation of a caldera. Eruptions that last longer are more likely to
302 end due to chamber underpressure and less likely to form a caldera. Figure 6a is a
303 histogram of caldera radii, which we assume to be equal to the chamber radius at
304 the time of caldera formation. The calderas formed by our model most frequently
305 have radii less than 2 km, although larger calderas can form. Figure 6b is a scat-
306 ter plot of caldera radius as a function of time of formation. The positive-sloping
307 trend of this plot implies that longer-lasting eruptions tend to form larger calderas,
308 as expected.

309 There are two other models for the future of the Lusi eruption. The first, by
310 Istadi et al. (2009) assumes an eruption rate and uses a GIS approach to account
311 for subsidence and ponding of mud on the surface. As it does not address the
312 controls of eruption rate and processes driving the mud to the surface we do not
313 discuss it further. This model does, however, address a feature of the eruption that
314 we neglect, namely the emplacement and redistribution of the mud after eruption.

315 Davies et al. (2011b) develop a model that is more similar in approach to our
316 own in that they model the mechanics of the eruption process and mass transport.
317 The model differs significantly, however, in the inferred source of the fluids that
318 mix with the mud, the plumbing system for the fluids and mud, and the driving
319 forces for the eruption. Davies et al. (2011b) assume that water from a deep
320 artesian carbonate aquifer flows upwards into the 15 cm-diameter borehole created
321 by drilling operations. At the depths of the mud source, 1.8-1.6 km, the water
322 exits the conduit, mixes with mud in something analogous to our mud chamber,
323 and then erupts. The driving mechanism is overpressure in the carbonate aquifer,
324 and water from this aquifer entrains mud and carries it to the surface. Our model

325 thus differs conceptually in two important respects: the importance of the deep
326 carbonate aquifer, and the driving forces. We have argued that a source of extra
327 fluid is not needed after the initial phases of the eruption. Without this additional
328 source of overpressure, our eruption is sustained by exsolution and expansion
329 of gases derived from the mud source region. We note that the 50th percentile
330 eruption duration predicted by Davies et al. (2011b) is 26 years, substantially less
331 than we predict without invoking an external fluid source. We expect that the
332 addition of an external source of fluids (and overpressure) to our model would
333 increase the duration of our model eruptions.

334 **8. Conclusions**

335 In summary, we considered two possible scenarios under which the current
336 eruption may end, either through the eventual inability of dissolved gases to sus-
337 tain the eruption, or the formation of a caldera. We made some necessary simpli-
338 fications in order to develop a tractable model, most importantly the assumption
339 of constant conduit geometry and uniform material properties of the mud source
340 and surroundings. There is also considerable uncertainty in mechanical proper-
341 ties such as viscosity, failure strength of the mud, initial gas content, and origin
342 of additional fluids. However, once we constrain the model to produce the ob-
343 served eruption rate, uncertainty in viscosity and gas content have little effect on
344 longevity predictions.

345 Validating our conceptual model is necessary for its predictions to be relevant
346 and useful for planning. It should be possible to demonstrate the existence and
347 amount of additional fluids (Davies et al., 2007, 2011b) by sampling fluids from
348 the mud source and deeper aquifers, and comparing these with samples of the

erupted mud. There is also some ambiguity in the measurements of gas composition, and the collection of gas samples directly from Lusi's crater would better inform our model parameters. We have also neglected to include aspects of regional tectonics that may influence the eruption, particularly if the mud source expands. Perhaps most important is the role of stresses from the reactivated Watukosek fault that passes through the eruption source (Mazzini et al., 2009). The spatial correlation of mud volcano locations with the fault suggests that the fault influences at least the location of the eruptions. Our treatment of mud rheology and mobilization is simplified, as mud failure and flow are complicated. Finally, our treatment of the region surrounding the mud chamber as elastic cannot account for surface cracks and motion on nearby faults, features that suggest brittle failure or plastic deformation. Despite the uncertainties in material properties and the model approximations, our modeling framework allows us to make probabilistic estimates of longevity and to highlight how predictions can be improved in light of better observational constraints.

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Symbol	Value (or Mean)	Standard Deviation	Description
$\log_{10}(E \text{ (Pa)})$	8	1	Young's modulus
ν	0.15	0.1	Poisson's ratio
$\log_{10}(\sigma_{y, \text{chamber}} \text{ (Pa)})$	6	1	Yield strength of mud source layer
$\sigma_{y, \text{caldera}}$	$10 \sigma_{y, \text{chamber}}$	N/A	Yield strength of near-surface material
μ	10^4 Pa s	N/A	Viscosity in conduit
r	1.4 m	N/A	Conduit radius
$[\text{CH}_4]$	0.5 wt %	N/A	Methane mole fraction
$[\text{CO}_2]$	1 wt %	N/A	CO_2 mole fraction

Table 1: Summary of the values for model parameters. The means and standard deviations listed were used in our Monte Carlo simulations.

Prior PDF Shape	Gaussian	σ boxcar	2σ boxcar
33% Longevity (years)	21	27	14
50% Longevity (years)	40	50	25
75% Longevity (years)	84	>100	52

Table 2: Summary of model results for both choices of gas composition and different assumptions about the distribution of model unknowns. Models with gaussian pdfs use the means and standard deviations shown in Table 1. Models with σ -boxcar and 2σ -boxcar distributions use mean values and standard deviations (σ) from Table 1 and assume a flat pdf within σ or 2σ of the mean.

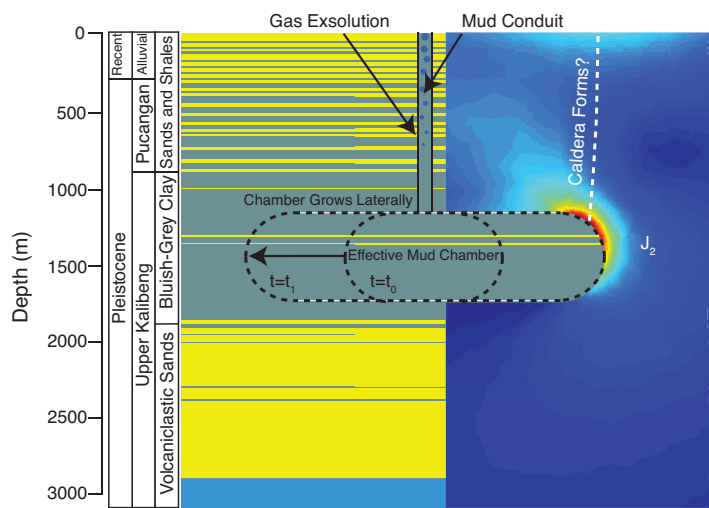


Figure 1: An illustration of model geometry and how it relates to subsurface lithology, (left of conduit) and our calculated J_2 (second deviatoric stress invariant), right of conduit. Warmer colors indicate larger values of J_2 . Stratigraphy is adopted from (Mazzini et al., 2007) and is based on logs of BJP1.

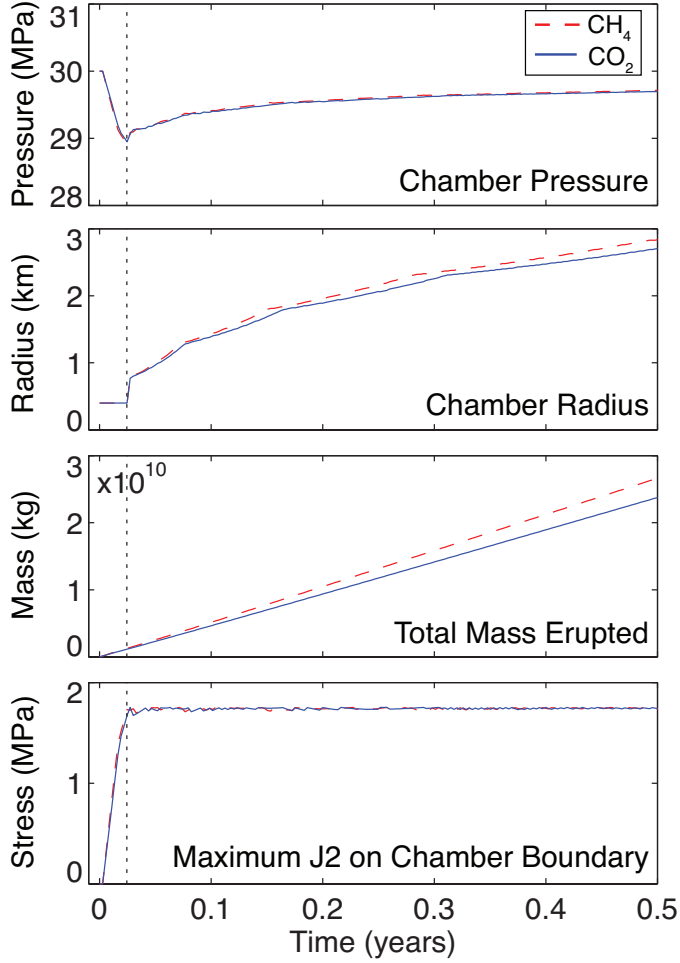


Figure 2: Temporal plots of chamber pressure, chamber (mobilized region) radius, cumulative mass erupted, and maximum J_2 on the chamber boundary (top to bottom). The red dashed lines are from a model in which we used 0.5 mol % CH₄ while the blue curves are for a model with 1 mol % CO₂. The two models are otherwise identical. The most important feature of the model results, illustrated here, is that once yielding begins (indicated by dashed vertical line), there is a drastic change in system behavior. Chamber radius begins to increase, and chamber pressure is buffered by the incorporation of material with higher pore pressure than that of the material filling the chamber prior to expansion. Like chamber pressure, mass flux is buffered and varies only by about 1% and J_2 remains constant at the value of the yield strength ($\tau_{y, \text{chamber}}$).

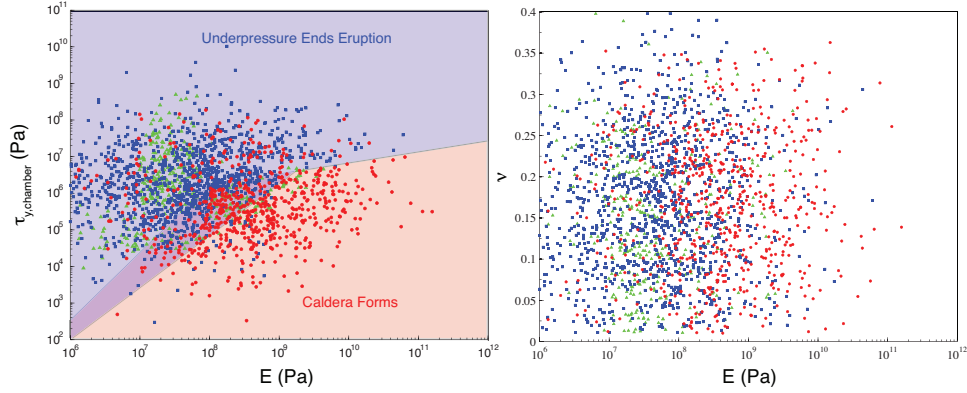


Figure 3: Regime diagram illustrating effect of variables on model outcome (gaussian model). Each glyph represents one model realization and colors/shapes correspond to outcomes: blue squares - insufficient chamber pressure ends eruption, red circles - caldera forms, green triangles - eruption lasts longer than 100 years.

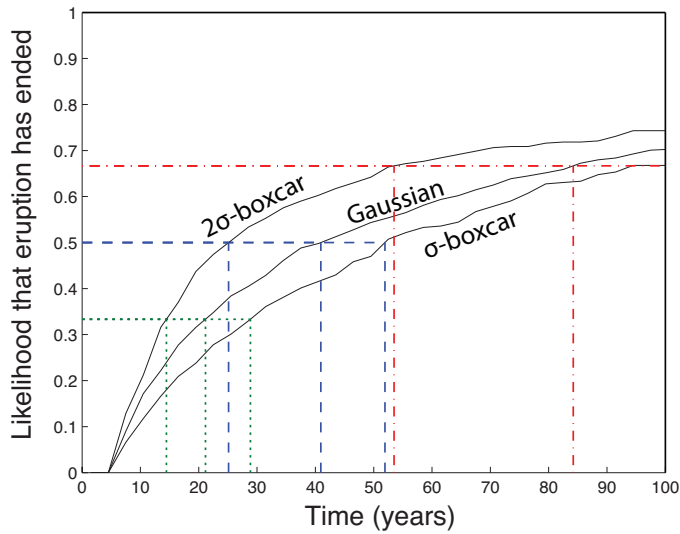


Figure 4: Cumulative probability that the eruption has ended for all three distributions of unknown variables. Horizontal axis is time since eruption started, vertical axis is likelihood that eruption will have ended or formed a caldera. Green dotted, blue dashed, and red dot-dashed lines indicate times at which likelihood is 1/3, 1/2, and 2/3, respectively.

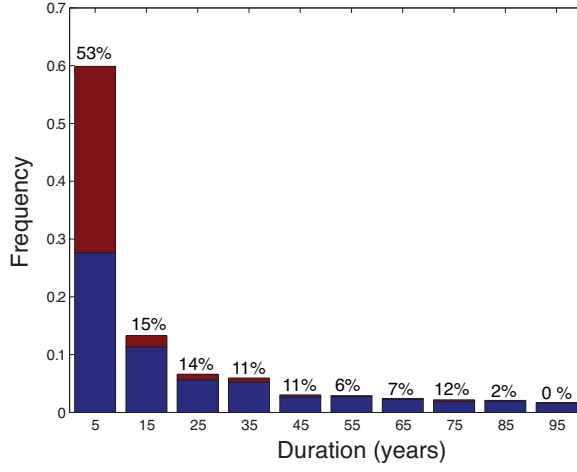


Figure 5: Histogram of eruption durations for gaussian model. Red bars indicate eruptions that formed a caldera and blue bars indicate eruptions that ended due to insufficient chamber pressure. We list the percentage of the eruptions in a given bin that ended due to caldera formation.

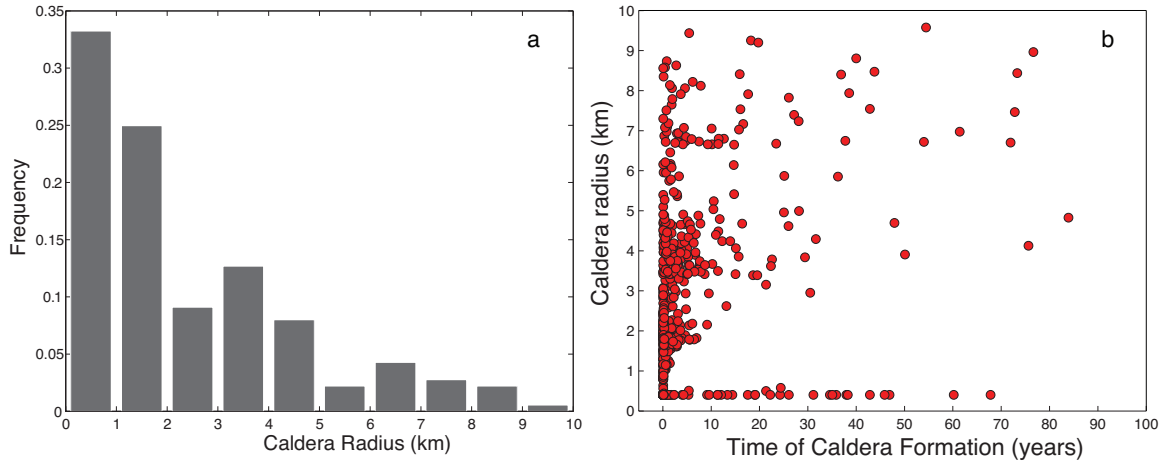


Figure 6: (a) Histogram of caldera radii for gaussian model. Frequency of radii of caldera formed in the model, normalized so that bins sum to 1. (b) Relationship between caldera radius and time of formation.